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(/)
KCL KVL
VCR



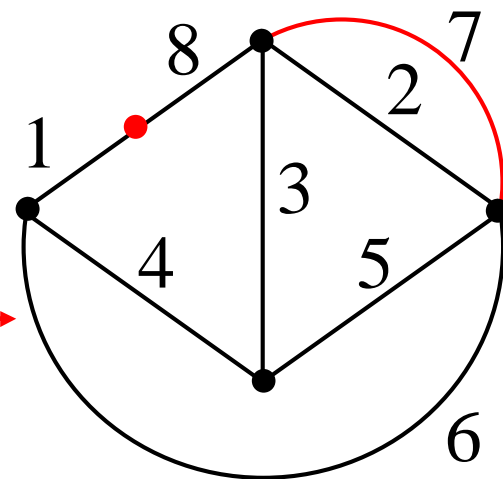
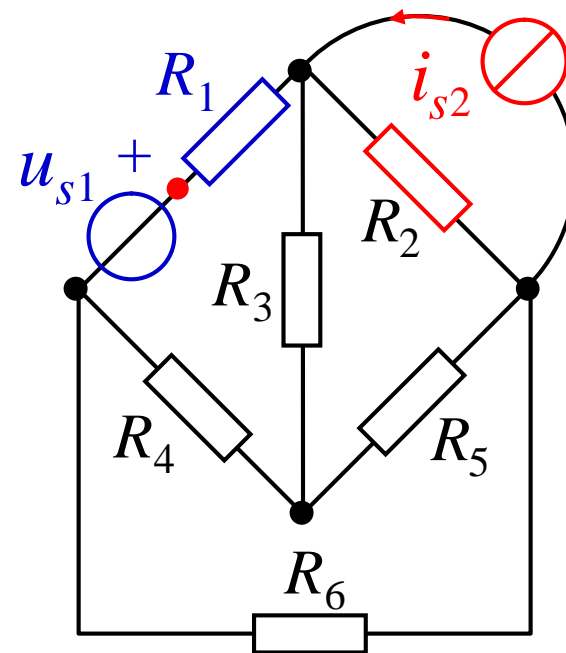


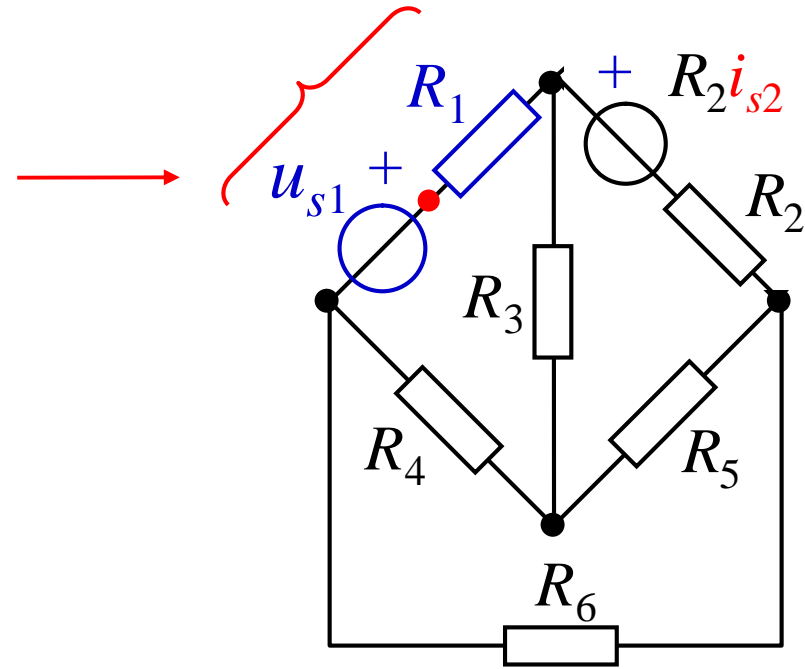
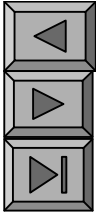
G

“(Graph)”

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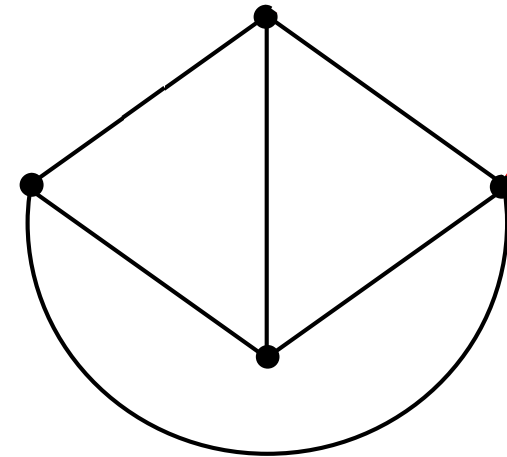


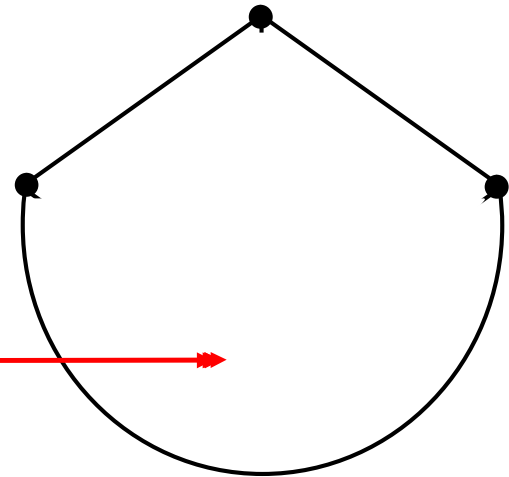
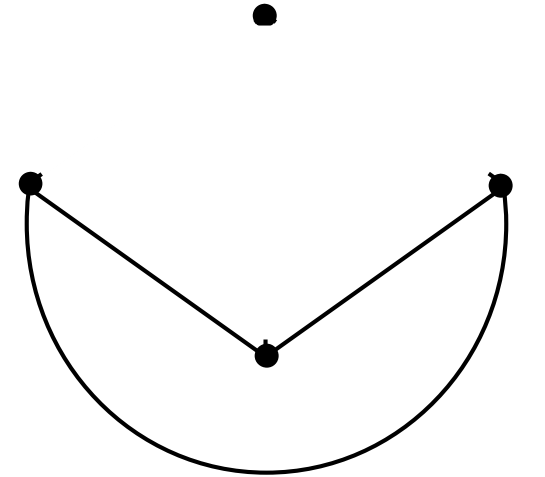
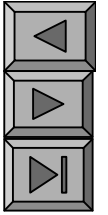


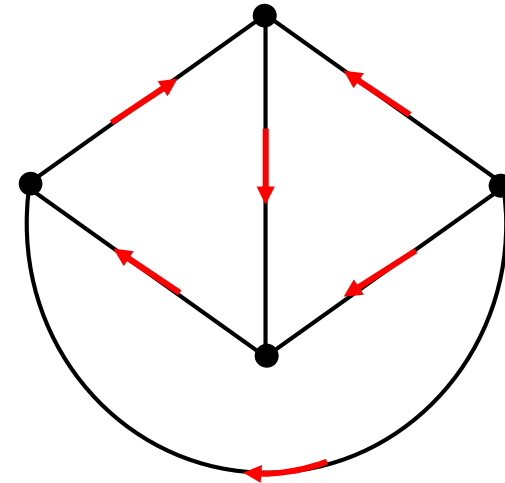
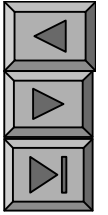
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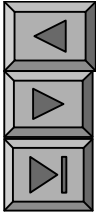




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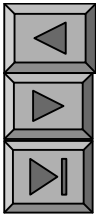
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3 2 KCL KVL

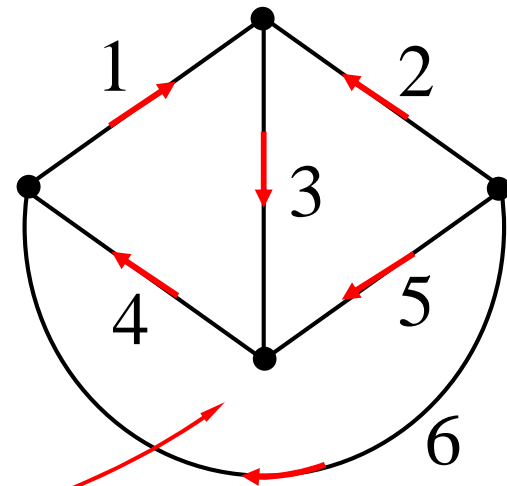


KCL

-

LVL

$$\begin{aligned}
 \cancel{i_1} + \underline{i_4} + \cancel{i_6} &= 0 \\
 \cancel{i_1} + \cancel{i_2} + \underline{i_3} &= 0 \\
 \cancel{i_2} + \underline{i_5} + \cancel{i_6} &= 0 \\
 \underline{i_3} + \underline{i_4} + i_5 &= 0
 \end{aligned}$$



- 4

0

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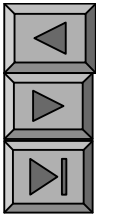
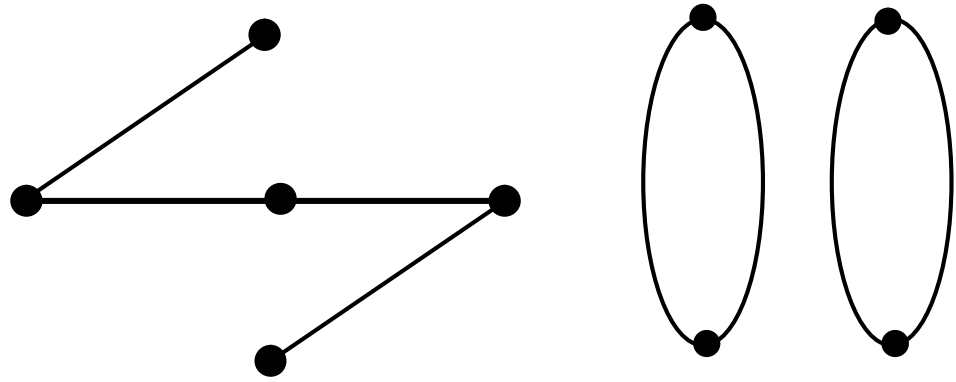
1.

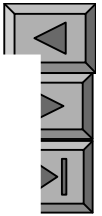
()



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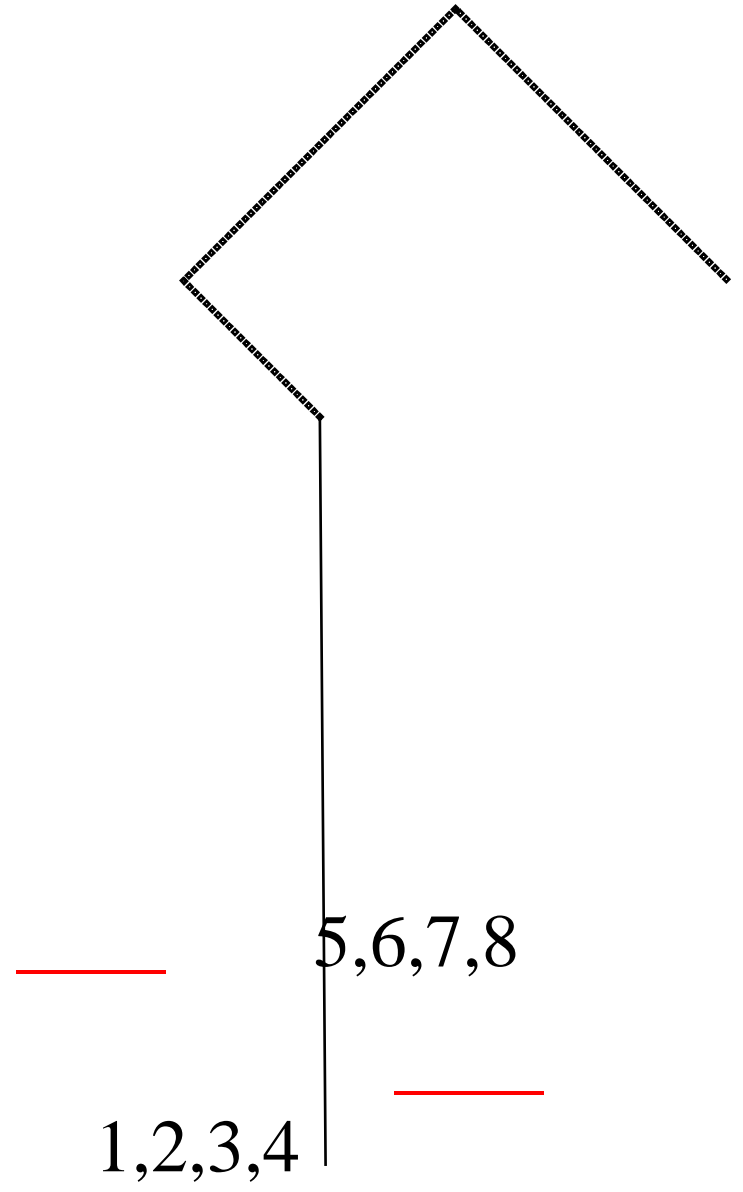
G

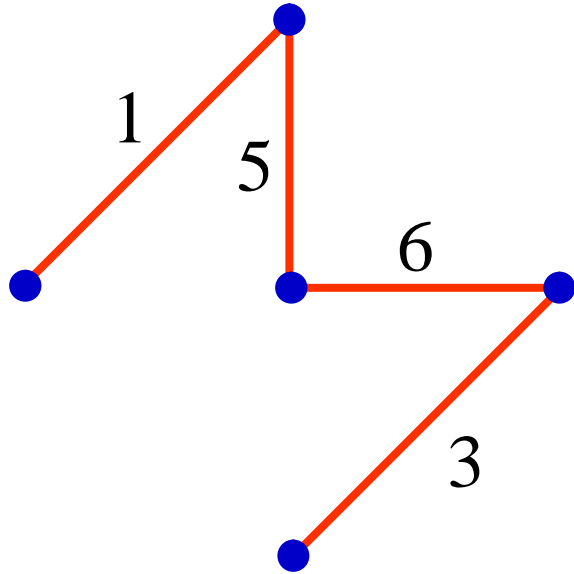
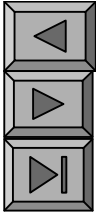




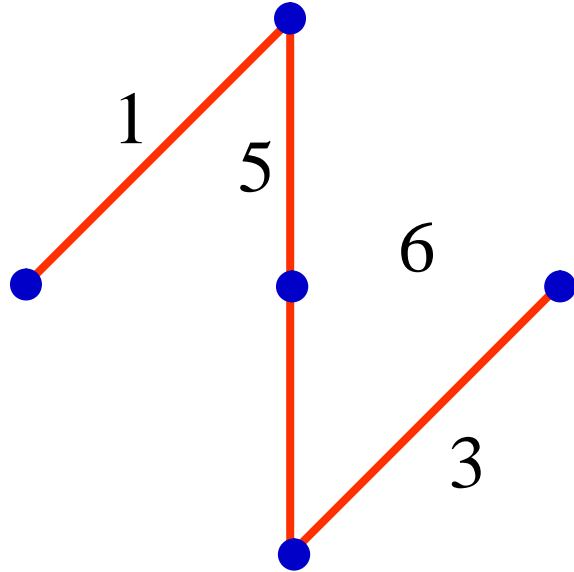
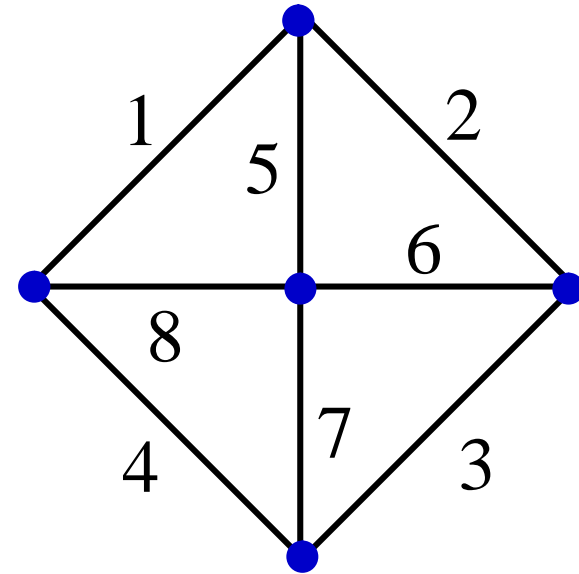
G
(1,5,8) (2,5,6) (1,2,3,4)
• 13
13

2. (Tree)
G T
G
G





T



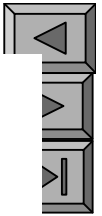
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G 5
T

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n
 $(n - 1)$

4



G
 $n (=5)$

-
-

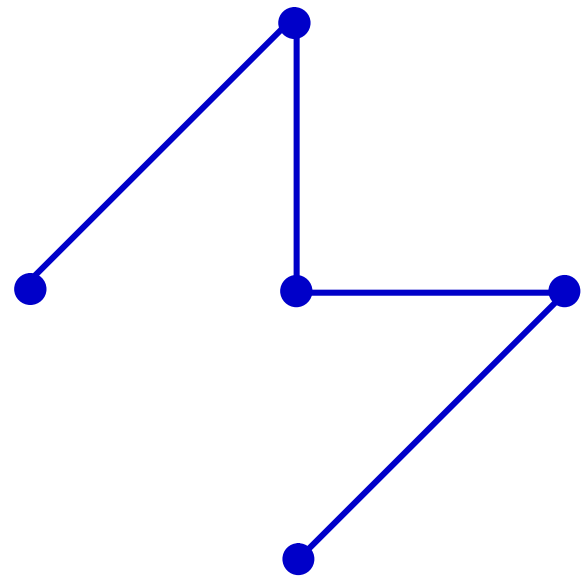
1

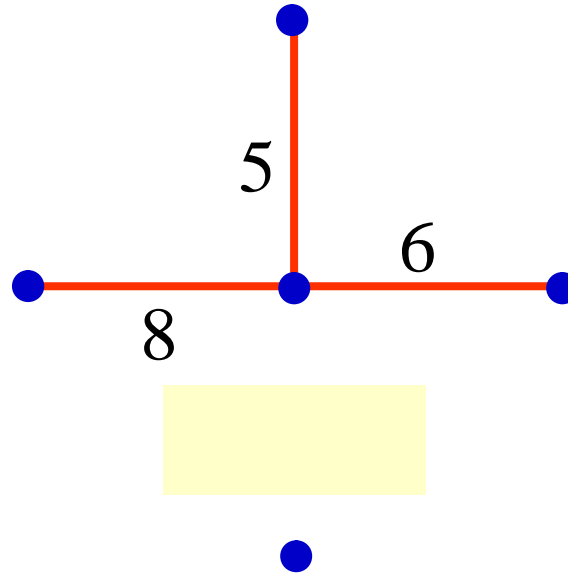
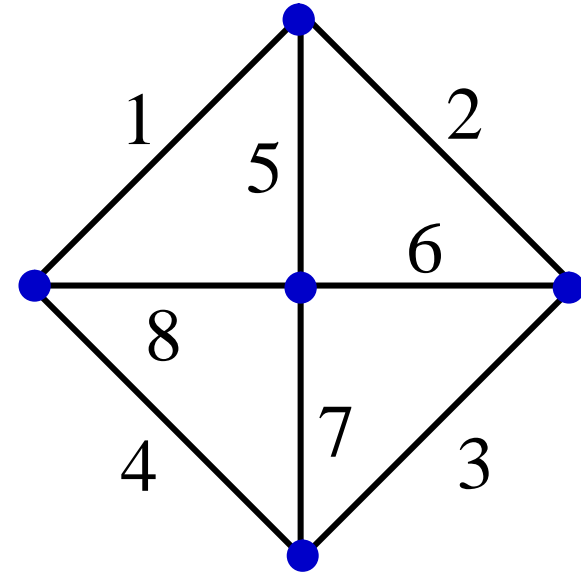
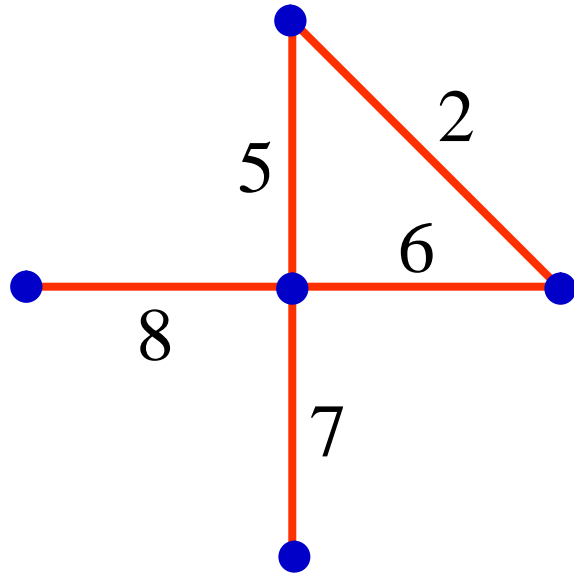
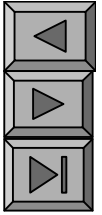
G
2

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$n (=5)$

$(n - 1 = 4)$





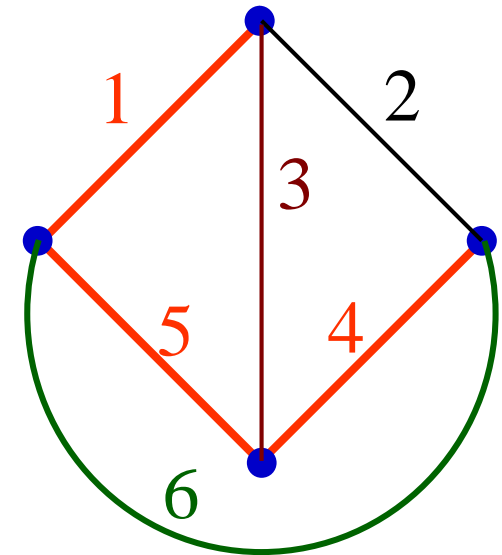
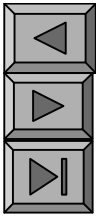
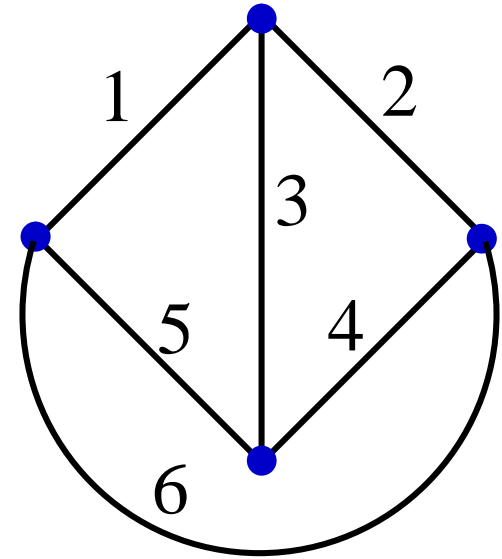
3.

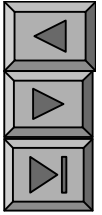


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$G \quad n \quad b$

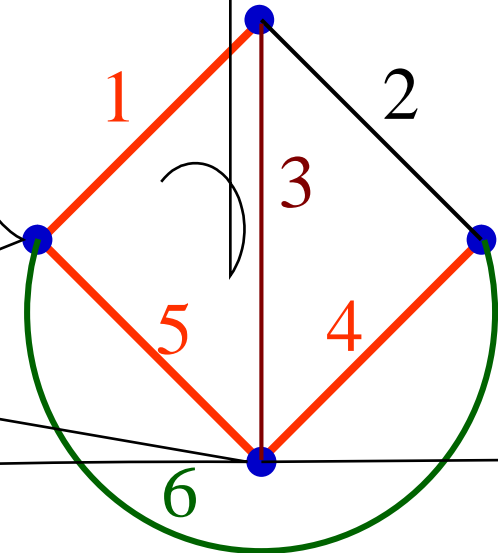
G

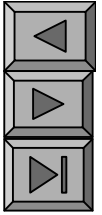
$(n - 1)$

$b \quad (n - 1)$

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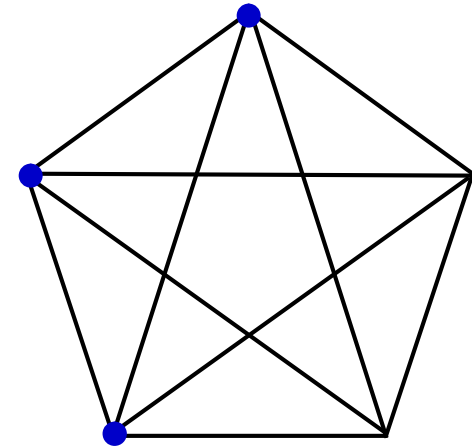
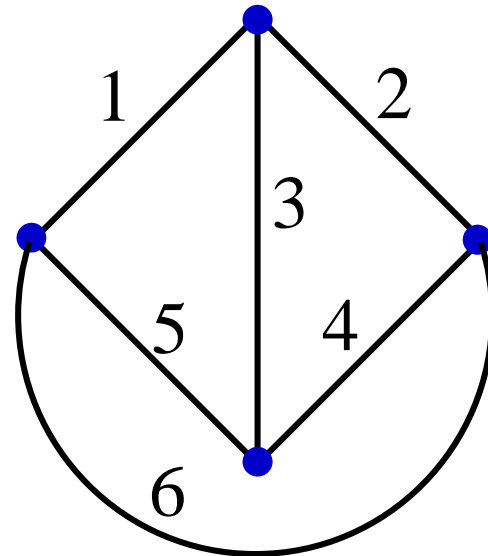
$l = b \quad (n - 1)$





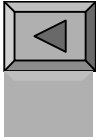
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$$l = b - (n - 1)$$

➤ KVL



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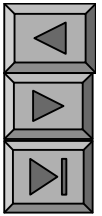
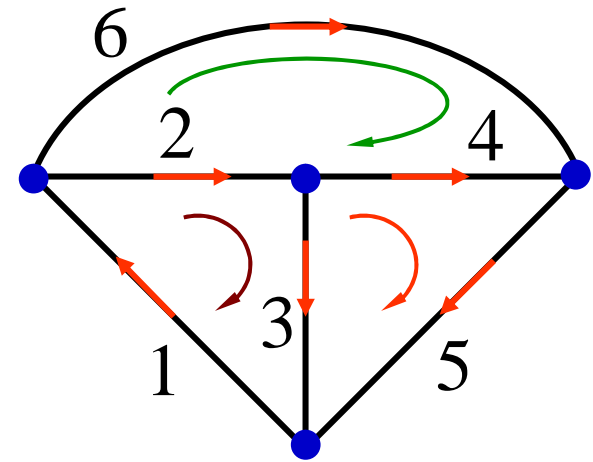
•

b :

KCL: $(n-1)$
KVL: $(b-n+1)$ } b

VCR: b

n



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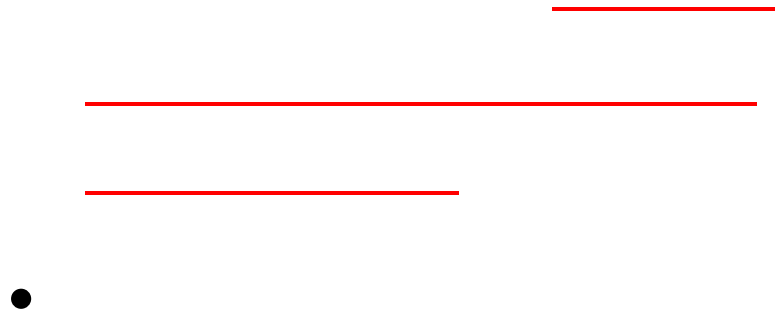
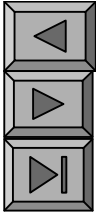
$2b$

•

$2b$

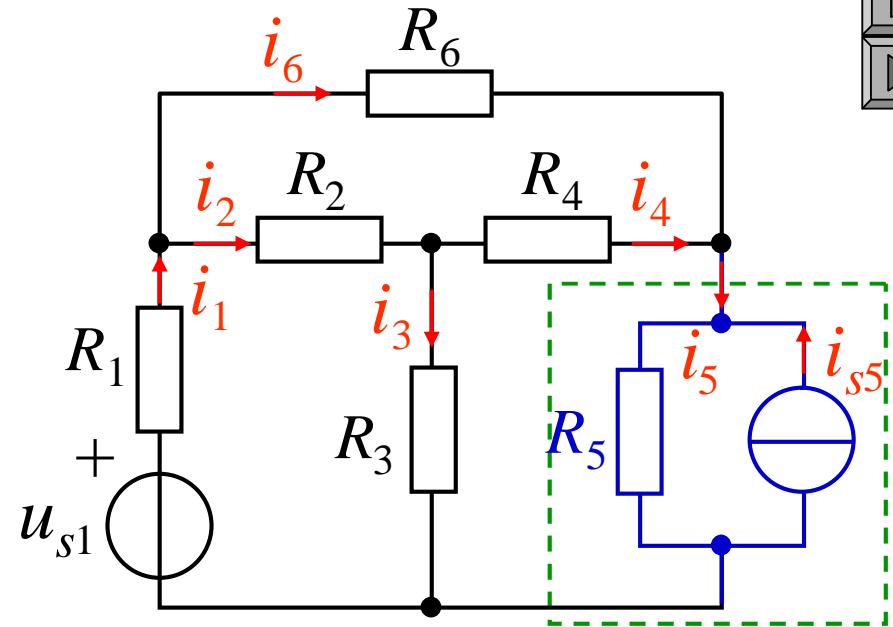
$2b$

$2b$



$2b$

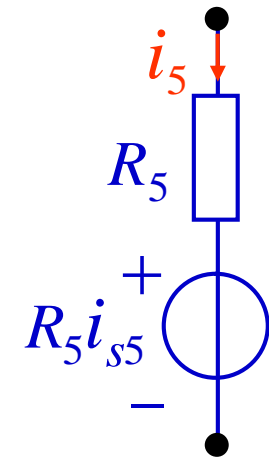
b



VAR

KCL KVL

1.
(1)



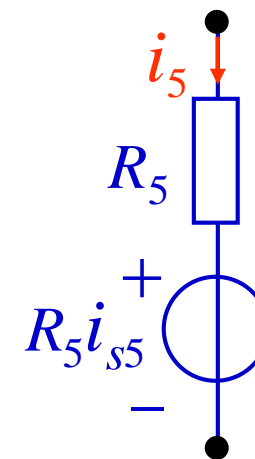
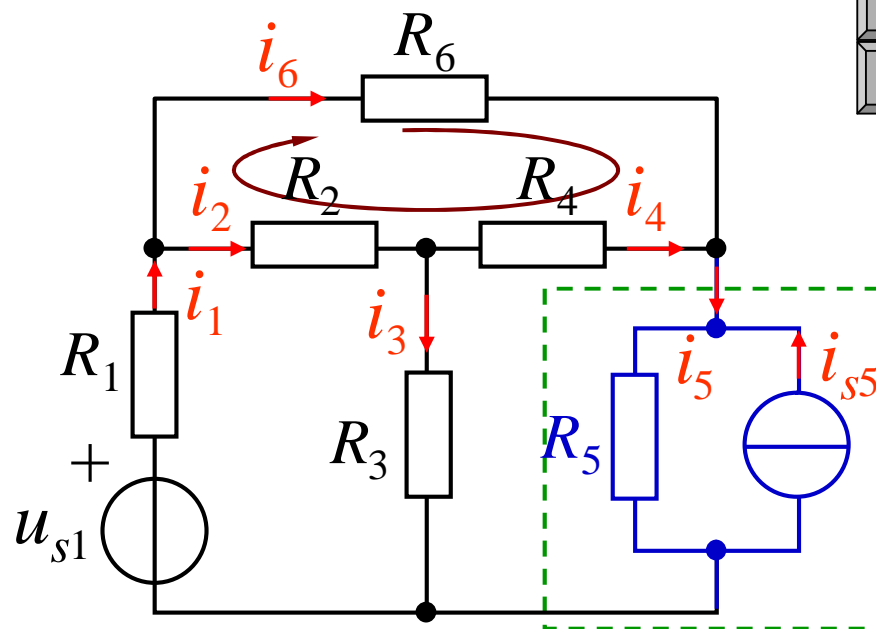


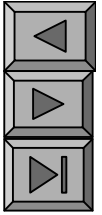
(2) KCL ($n - 1$)

$$\begin{aligned} &: -i_1 + i_2 + i_6 = 0 \\ &: -i_2 + i_3 + i_4 = 0 \\ &: -i_4 + i_5 - i_6 = 0 \end{aligned}$$

(3) ($b - n + 1$)

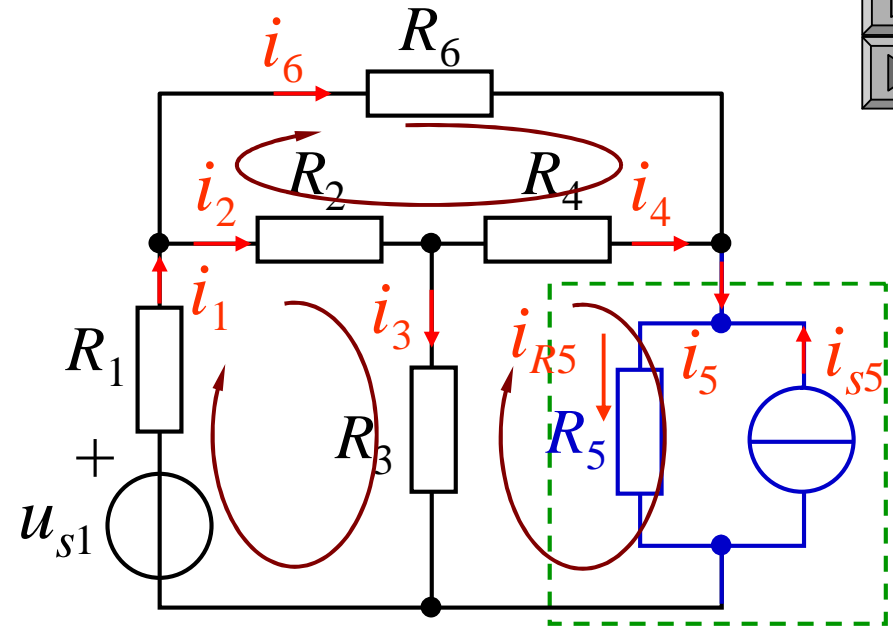
KVL





$$\begin{aligned}
 -i_1 + i_2 + i_6 &= 0 \\
 -i_2 + i_3 + i_4 &= 0 \\
 -i_4 + i_5 - i_6 &= 0 \\
 R_1 i_1 + R_2 i_2 + R_3 i_3 &= u_{s1} \\
 -R_3 i_3 + R_4 i_4 + R_5 i_5 &= -R_5 i_{s5} \\
 -R_2 i_2 - R_4 i_4 + R_6 i_6 &= 0
 \end{aligned}$$

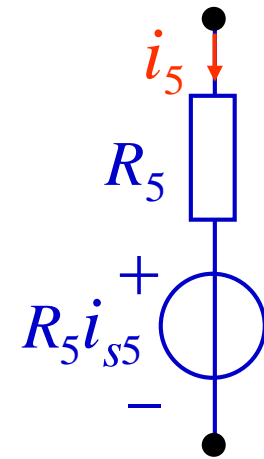
(4) i_1 i_6

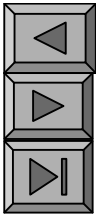


R_5

$$u_{14} = u_{s1} - R_1 i_1$$

$$i_{R5} = i_{s5} + i_5$$

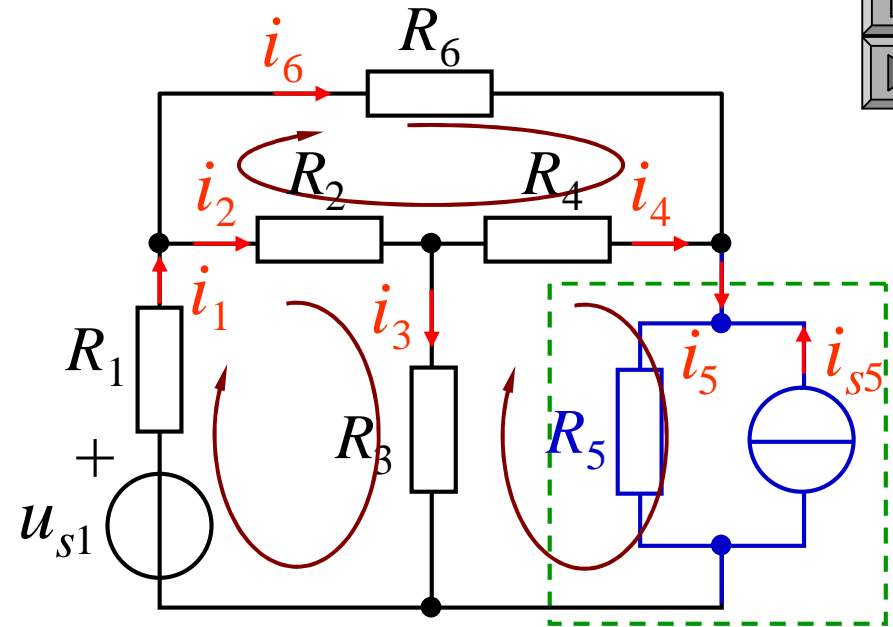




KVL

$$\begin{aligned}
 R_1 i_1 + R_2 i_2 + R_3 i_3 &= u_{s1} \\
 -R_3 i_3 + R_4 i_4 + R_5 i_5 &= -R_5 i_{s5} \\
 -R_2 i_2 - R_4 i_4 + R_6 i_6 &= 0
 \end{aligned}$$

$$R_k i_k = u_{sk}$$



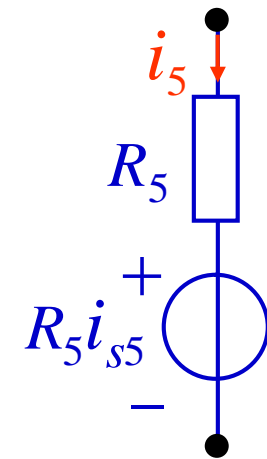
- i_k

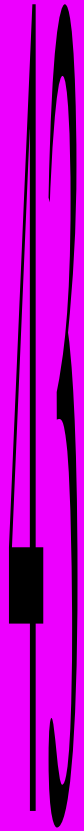
-

u_{sk}

$R_k i_k$

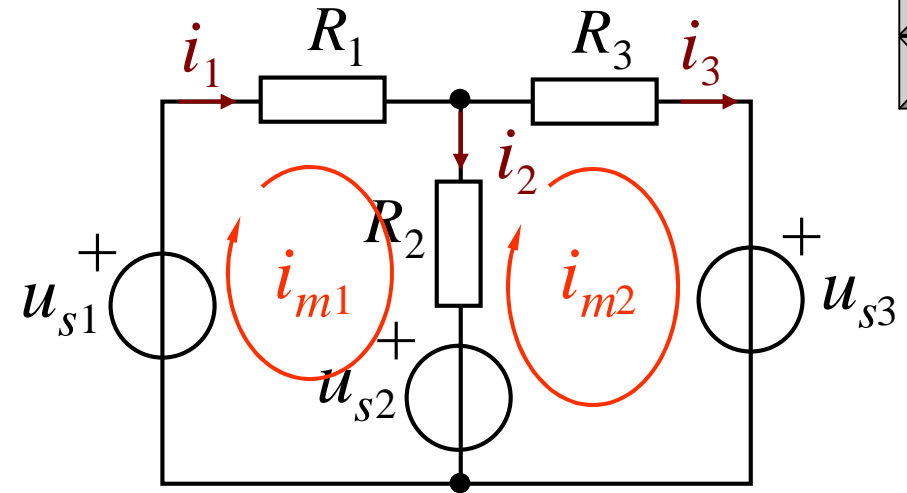
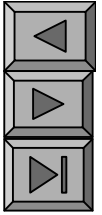
u_{sk}





KVL

2010 3 3



KVL

1.

(1)

(2)

KVL

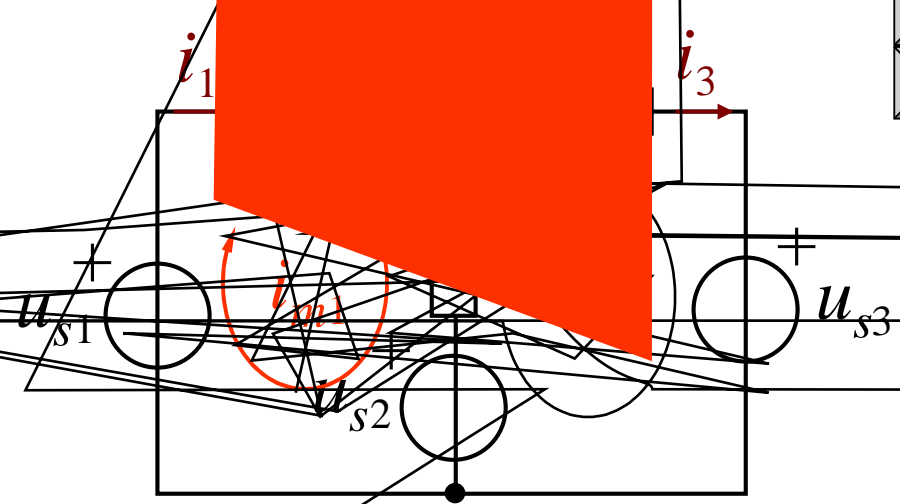
i_{m1} i_{m2} R_2

$$1 \quad R_1 i_{m1} + R_2 i_{m1} - R_2 i_{m2} = u_{s1} - u_{s2}$$

$$2 \quad R_2 i_{m1} - R_2 i_{m2} + R_3 i_{m2} = u_{s2} - u_{s3}$$

$$R_{11}i_{m1} + R_{12}i_{m2} = u_{s11}$$

$$R_{21}i_{m1} + R_{22}i_{m2} = u_{s22}$$



$$R_1 i_{m1} + R_2 i_{m1} - R_2 i_{m2} = u_{s1} - u_{s2}$$

$$R_2 i_{m1} + R_2 i_{m2} + R_3 i_{m2} = u_{s2} - u_{s3}$$

$$(R_1 + R_2) i_{m1} - R_2 i_{m2} = u_{s1} - u_{s2}$$

$$R_2 i_{m1} + (R_2 + R_3) i_{m2} = u_{s2} - u_{s3}$$

$$R_{11}i_{m1} + R_{12}i_{m2} = u_{s11}$$

$$R_{21}i_{m1} + R_{22}i_{m2} = u_{s22}$$

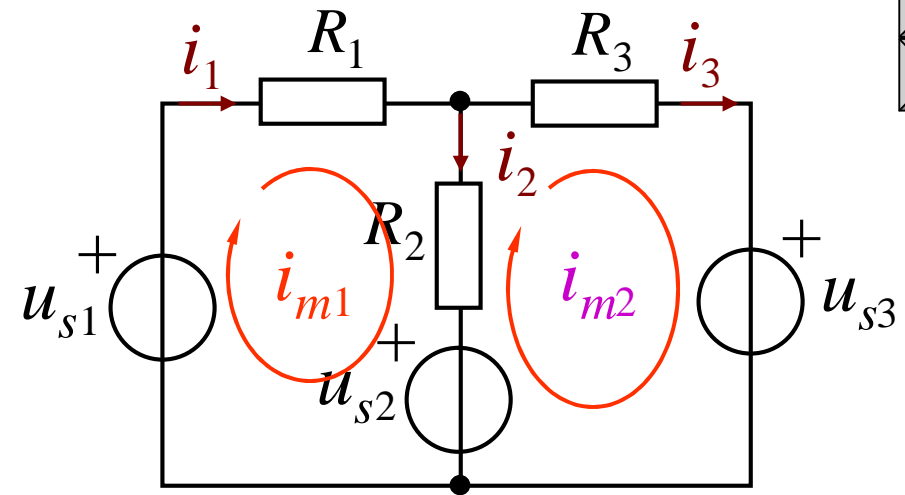
$$R_{12}i_{m2} \quad i_{m2} \quad 1$$

$$R_{21}i_{m1} \quad i_{m1} \quad 2$$

$$R_{12} \quad R_{21}$$

$$i_{m2} \quad (i_{m1})$$

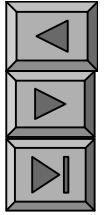
$$R_{12} = R_{21} = R_2$$



1 (2)

$$(R_1 + R_2)i_{m1} - R_2i_{m2} = u_{s1} - u_{s2}$$

$$R_2i_{m1} + (R_2 + R_3)i_{m2} = u_{s2} - u_{s3}$$



2. m

$$R_{11}i_{m1} + R_{12}i_{m2} + R_{13}i_{m3} + \dots + R_{1m}i_{mm} = u_{s11}$$

$$R_{21}i_{m1} + R_{22}i_{m2} + R_{23}i_{m3} + \dots + R_{2m}i_{mm} = u_{s22}$$

$$R_{31}i_{m1} + R_{32}i_{m2} + R_{33}i_{m3} + \dots + R_{3m}i_{mm} = u_{s33}$$

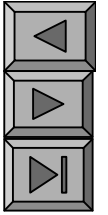
.....

$$R_{m1}i_{m1} + R_{m2}i_{m2} + R_{m3}i_{m3} + \dots + R_{mm}i_{mm} = u_{smm}$$

- R_{11} R_{mm} _____
- R_{12} R_{1m} R_{21} R_{m1}

(1)

“ ”



(2)

(3)

0

(4)

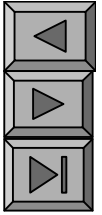
$$R_{ik} = R_{ki}$$

- u_{s11} u_{smm} 1 m

“+”

“ ”

3-1 (P60)



1. (T)

G

(1)

(2) G

(3)

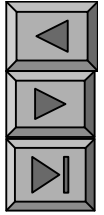
1

2. (L)

G

(1)

(2) 2



3. *KCL*

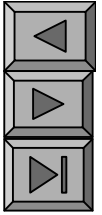
$$n-1$$

KVL

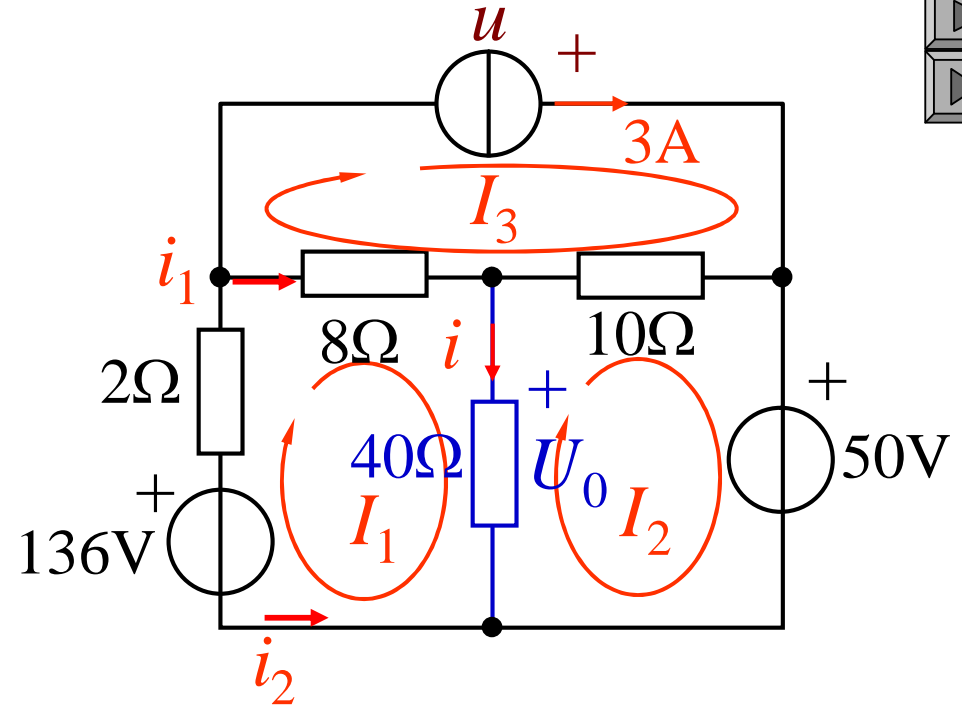
$$b - (n - 1)$$

4.

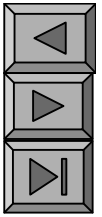
5.



$$i = I_1 - I_2$$
$$i_1 = I_1 - I_3$$
$$i_2 = -I_1$$



3-5



KVL



$$i_1 \quad i_2 \quad i_3$$

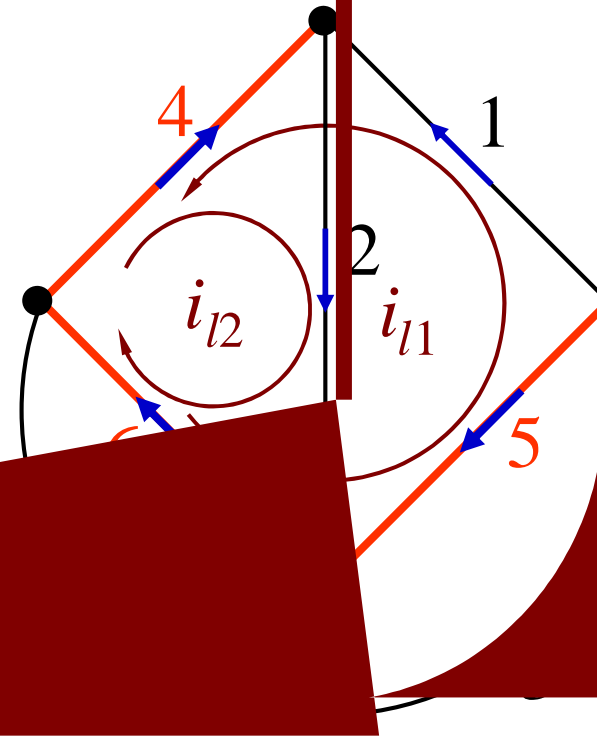
$$i_{l1} \quad i_{l2} \quad i_{l3}$$

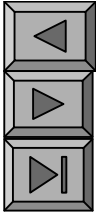
$$i_1 = i_{l1} \quad i_2 = i_{l2} \quad i_3 = i_{l3}$$

$$i_4 = i_{l1} + i_{l2}$$

$$i_5 = -i_{l1} - i_{l3}$$

$$i_6 = -i_{l1} + i_{l2} - i_{l3}$$





KCL

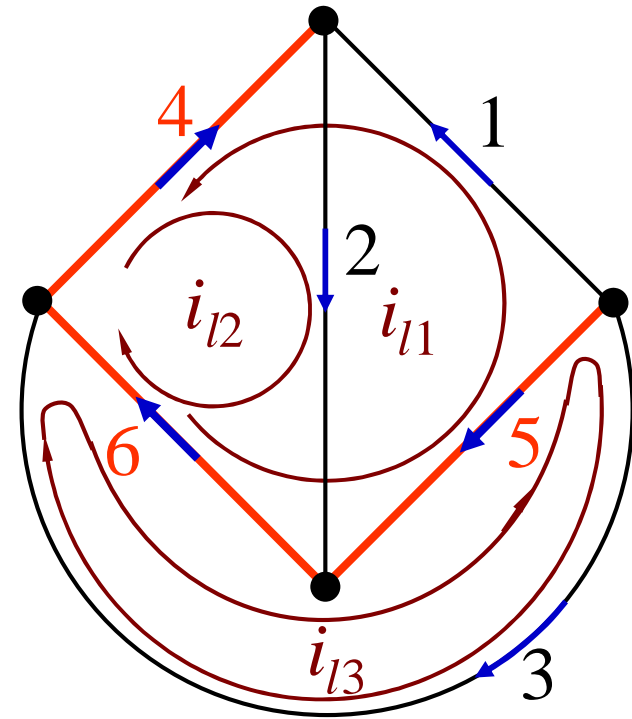
$$i_4 = -i_1 + i_2 = -i_{l1} + i_{l2}$$

$$i_5 = -i_1 - i_3 = -i_{l1} - i_{l3}$$

$$i_6 = -i_1 + i_2 - i_3 = -i_{l1} + i_{l2} - i_{l3}$$

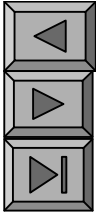
-
-

KCL



“ ”

()



1.

- b n ()
 $l = b$ ($n - 1$) KVL

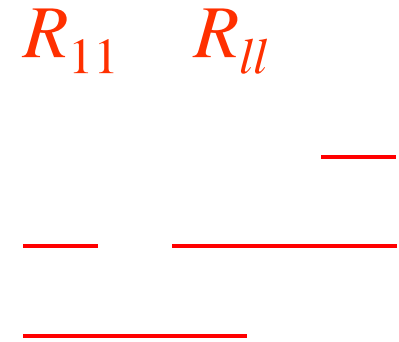
$$R_{11}i_{l1} + R_{12}i_{l2} + R_{13}i_{l3} + \dots + R_{1l}i_{ll} = u_{s11}$$

$$R_{21}i_{l1} + R_{22}i_{l2} + R_{23}i_{l3} + \dots + R_{2l}i_{ll} = u_{s22}$$

$$R_{31}i_{l1} + R_{32}i_{l2} + R_{33}i_{l3} + \dots + R_{3l}i_{ll} = u_{s33}$$

.....

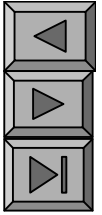
$$R_{l1}i_{l1} + R_{l2}i_{l2} + R_{l3}i_{l3} + \dots + R_{ll}i_{ll} = u_{sll}$$



$$R_{12} \quad R_{13} \quad R_{23} \quad R_{l1} \quad R_{l2}$$



“ ”

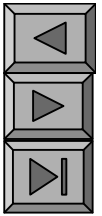
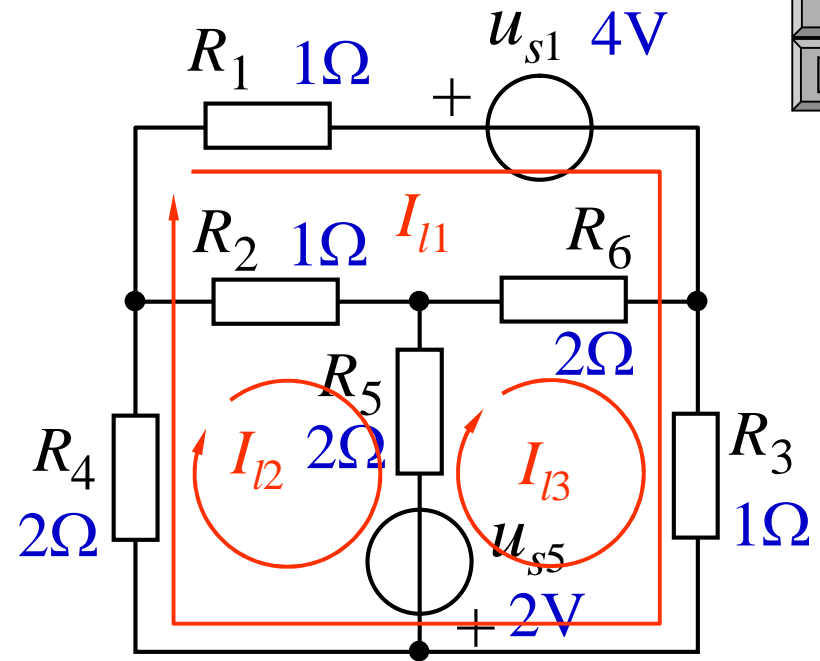


$$\begin{bmatrix} R_{11} & R_{12} & R_{13} & \cdots & R_{1l} \\ R_{21} & R_{22} & R_{23} & \cdots & R_{2l} \\ R_{31} & R_{32} & R_{33} & \cdots & R_{3l} \\ \cdots & \cdots & \cdots & \cdots & \cdots \\ R_{l1} & R_{l2} & R_{l3} & \cdots & R_{ll} \end{bmatrix} \begin{bmatrix} i_{l1} \\ i_{l2} \\ i_{l3} \\ \vdots \\ i_{li} \end{bmatrix} = \begin{bmatrix} u_{s11} \\ u_{s22} \\ u_{s33} \\ \vdots \\ u_{sll} \end{bmatrix}$$

$$u_{s11} \quad u_{sll} \quad 1 \quad l \quad 0$$

2.

P65 3 2



$$\left. \begin{aligned}
 \text{L1} \quad & 4I_{l1} + 2I_{l2} + 1I_{l3} = -4 \\
 \text{L2} \quad & 2I_{l1} + 5I_{l2} - 2I_{l3} = 2 \\
 \text{L3} \quad & 1I_{l1} - 2I_{l2} + 5I_{l3} = -2
 \end{aligned} \right\}$$

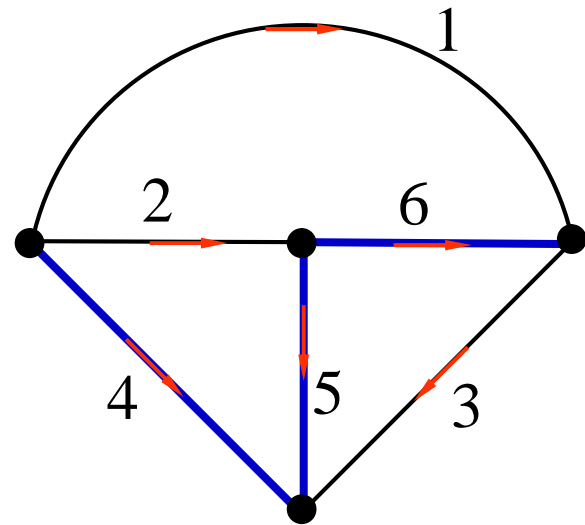
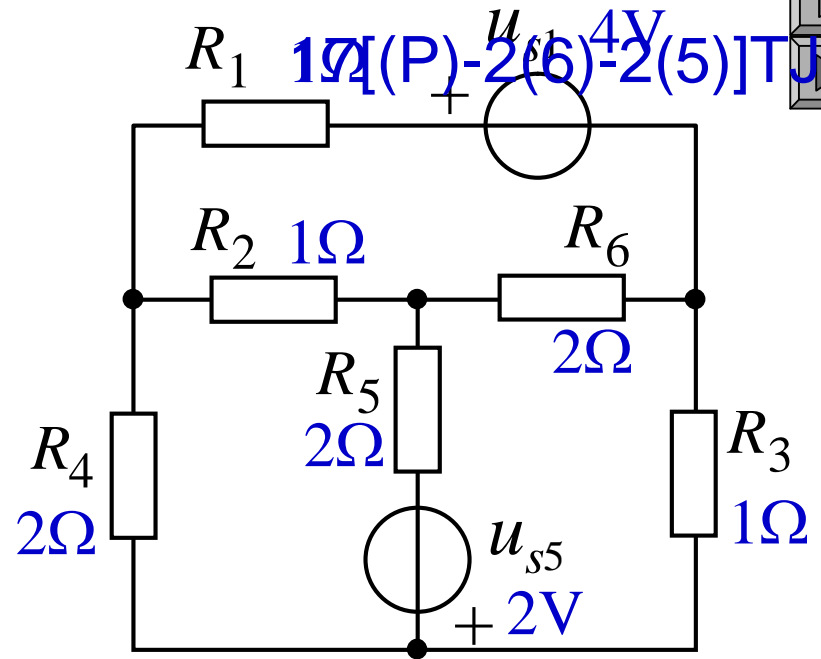
2.

P65

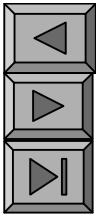
3 2



P65

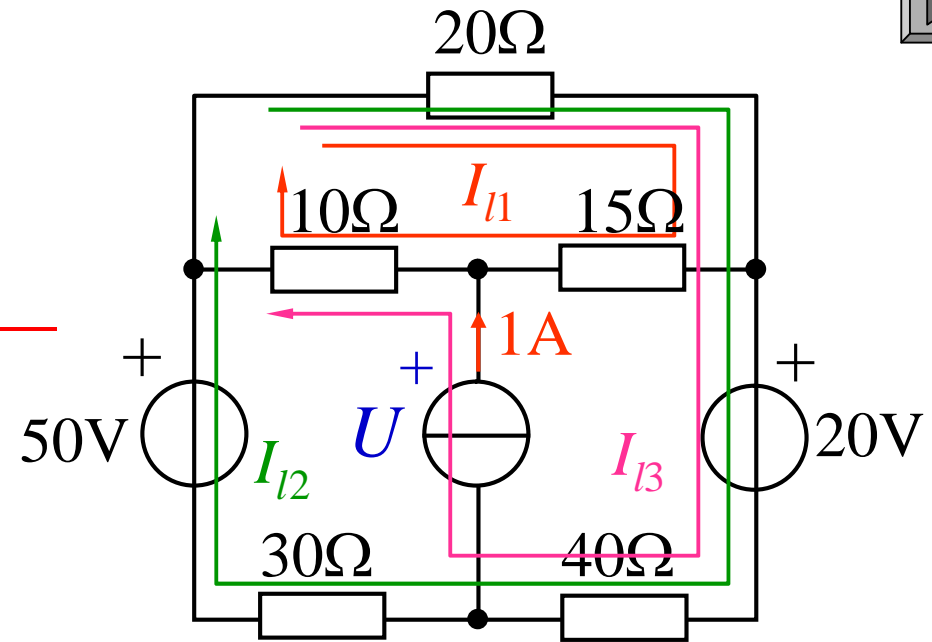


P67 3 3



(1)

(2)

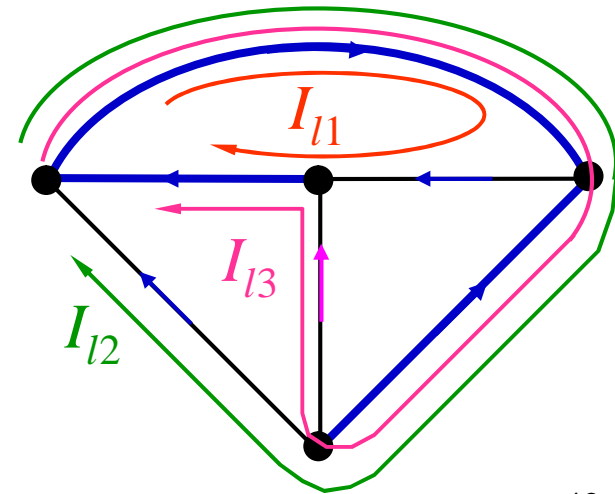


$$45I_{l1} + 20I_{l2} + 30I_{l3} = 0$$

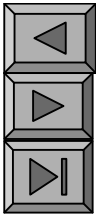
$$20I_{l1} + 90I_{l2} + 60I_{l3} = 30$$

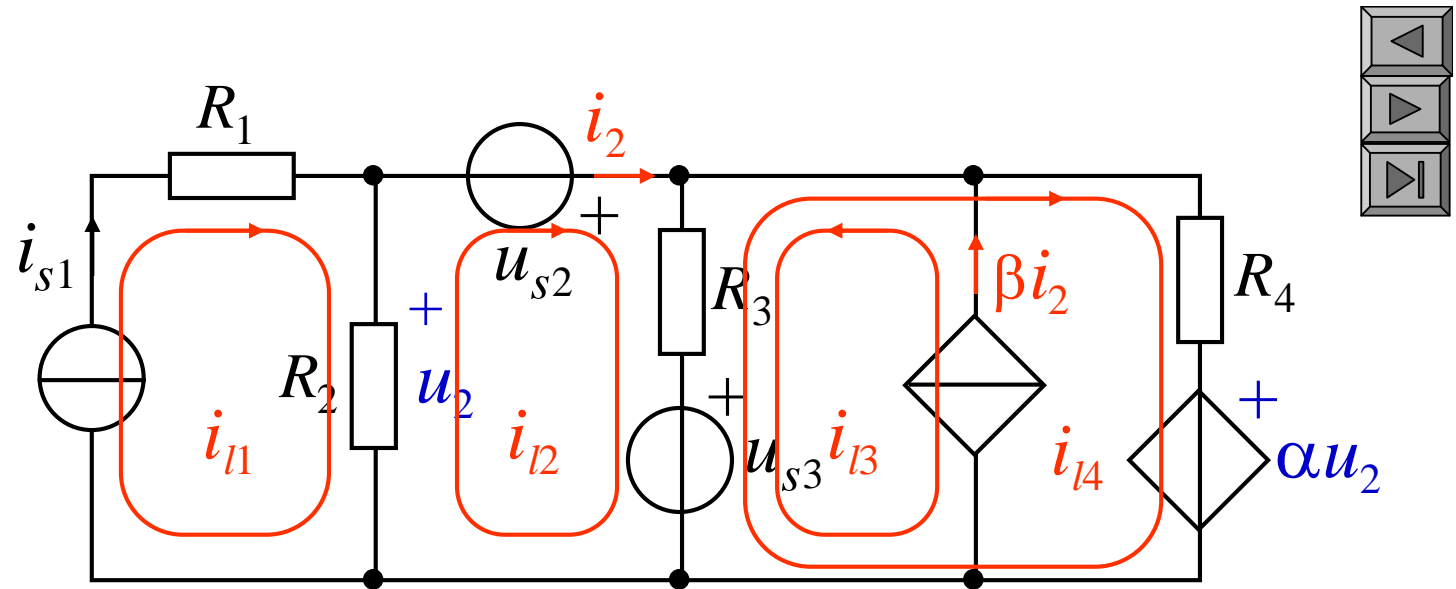
$$30I_{l1} + 60I_{l2} + 70I_{l3} = U - 20$$

$$I_{l3} = 1$$



P67-68 3 4





$$\text{L2} \quad \underline{-R_2 i_{l1} + (R_2 + R_3) i_{l2} + R_3 i_{l3} - R_3 i_{l4} = u_{s2} - u_{s3}}$$

$$\text{L4} \quad -R_3 i_{l2} - R_3 i_{l3} + (R_3 + R_4) i_{l4} = u_{s3} - \alpha u_2$$

1 3
KVL

$$\underline{i_{l1} = i_{s1}} \quad \underline{i_{l3} = \beta i_{l2}}$$

$$\alpha u_2 = \alpha R_2 (i_{l1} - i_{l2}) = \alpha R_2 i_{l1} - \alpha R_2 i_{l2}$$

$$\underline{\alpha R_2 i_{l1} - (\alpha R_2 + R_3) i_{l2} - R_3 i_{l3} + (R_3 + R_4) i_{l4} = u_{s3}}$$

3 6

•

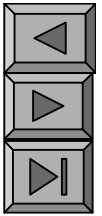
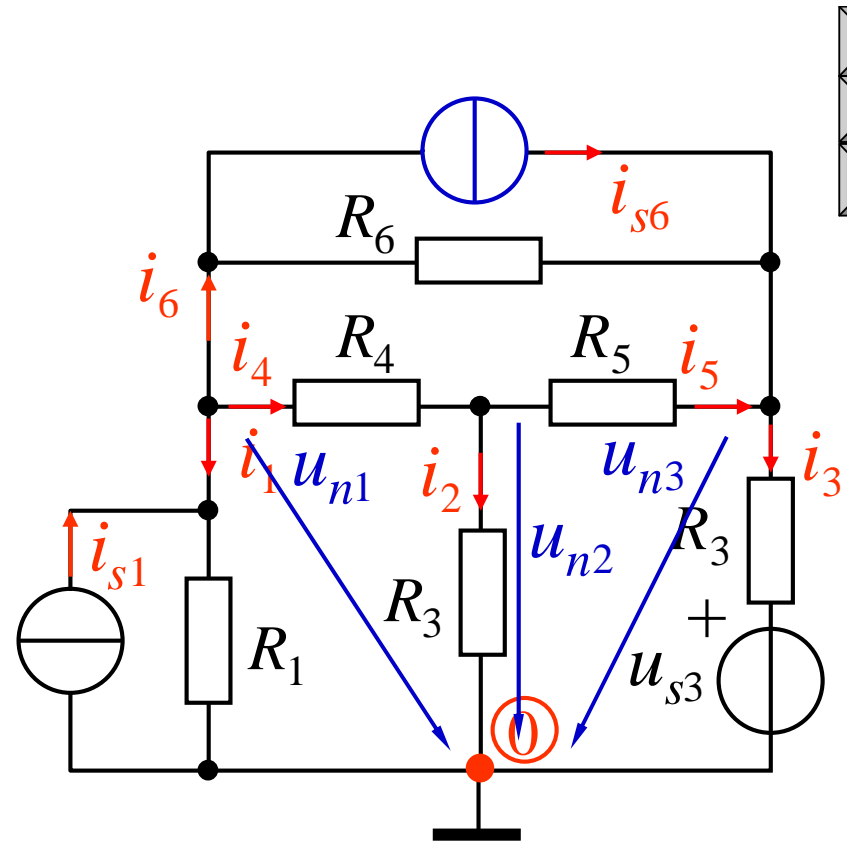
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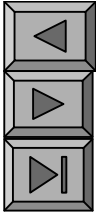
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n
)

$(n - 1)$

(





1.

•

• $u_{n1} = u_1 \quad u_{n2} = u_2 \quad u_{n3} = u_3$

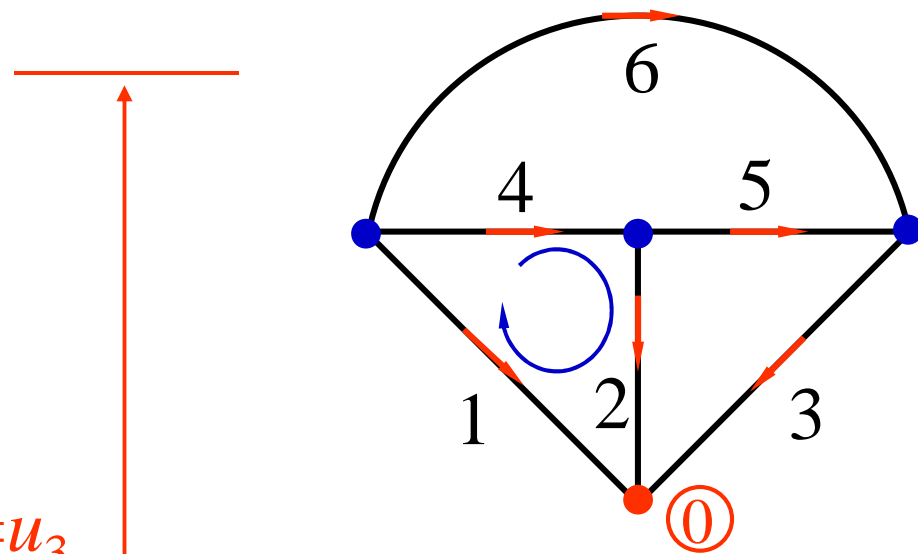
•

KVL $u_1 + u_4 + u_2 = 0$

$u_4 = u_1 \quad u_2 = u_{n1} \quad u_{n2}$

$u_5 = u_{n2} \quad u_{n3}$

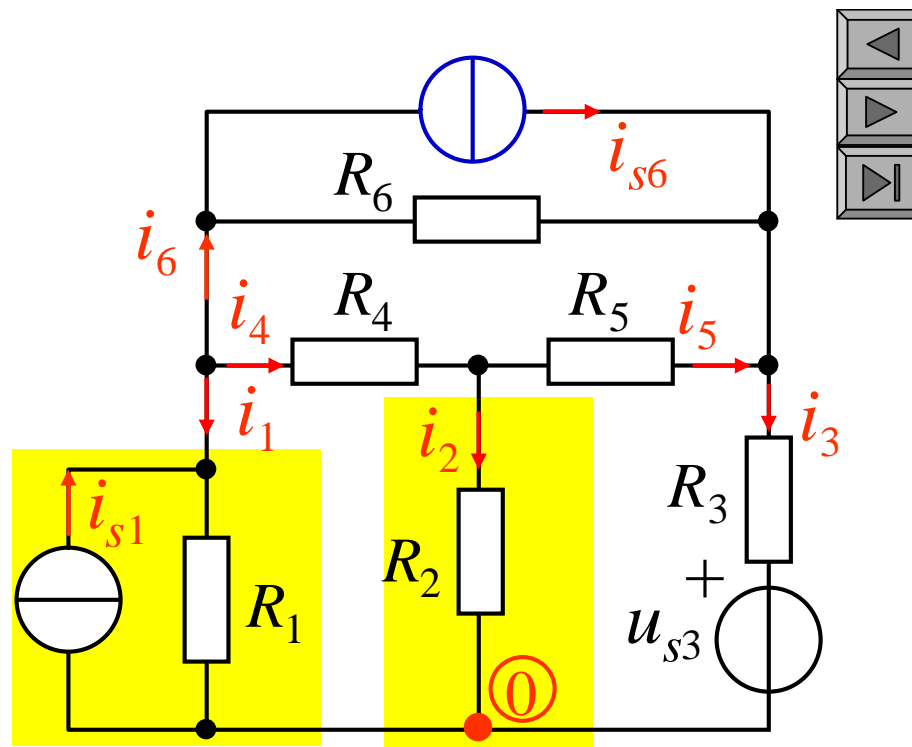
$u_6 = u_{n1} \quad u_{n3}$



$u_1 \quad u_6$
 $u_{n1} \quad u_{n3}$

2.

KCL !



$$i_1 = \frac{u_{n1}}{R_1} - i_{s1}$$

$$i_2 = \frac{u_{n2}}{R_2}$$

$$i_3 = \frac{u_{n3} - u_{s3}}{R_3}$$

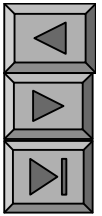
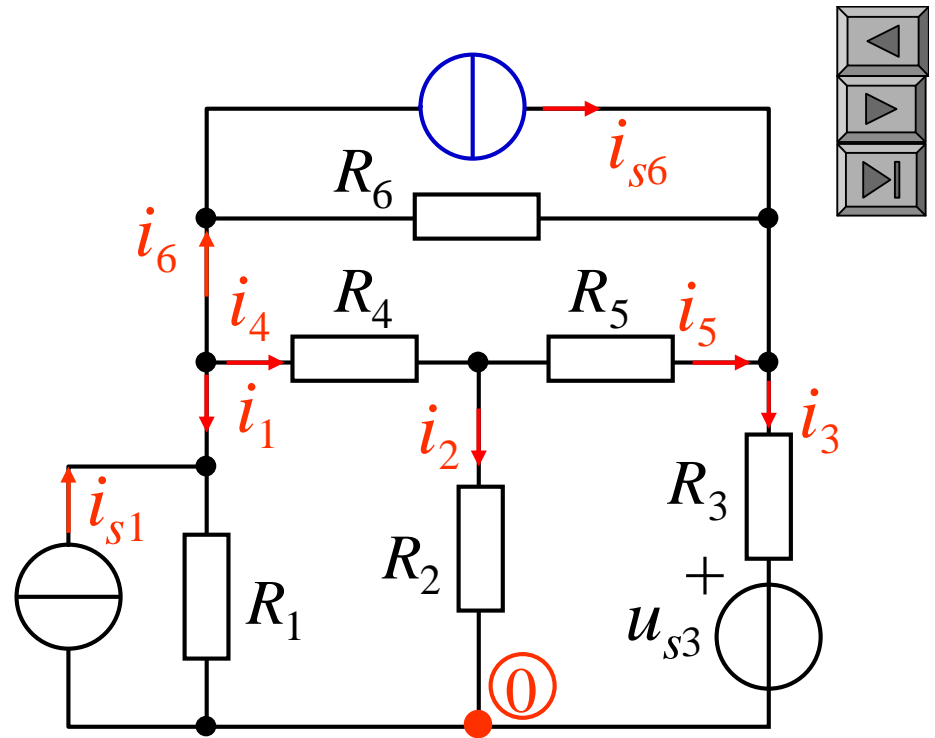
$$i_4 = \frac{u_{n1} - u_{n2}}{R_4}$$

$$i_5 = \frac{u_{n2} - u_{n3}}{R_5}$$

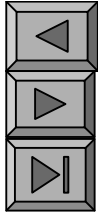
$$i_6 = \frac{u_{n1} - u_{n3}}{R_6} + i_{s6}$$

KCL:

$$\begin{cases} i_1 + i_4 + i_6 = 0 \\ i_2 + i_4 + i_5 = 0 \\ i_3 + i_5 + i_6 = 0 \end{cases}$$



3 i



$$\left[\frac{1}{R_1} + \frac{1}{R_4} + \frac{1}{R_6} \right] u_{n1} - \frac{1}{R_4} u_{n2} - \frac{1}{R_6} u_{n3} = i_{s1} - i_{s6}$$

$$- \frac{1}{R_4} u_{n1} + \left[\frac{1}{R_2} + \frac{1}{R_4} + \frac{1}{R_5} \right] u_{n2} - \frac{1}{R_6} u_{n3} = 0$$

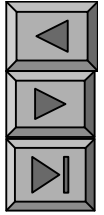
$$- \frac{1}{R_6} u_{n1} - \frac{1}{R_5} u_{n2} + \left[\frac{1}{R_3} + \frac{1}{R_5} + \frac{1}{R_6} \right] u_{n3} = i_{s6} + \frac{u_{s3}}{R_3}$$

$$\frac{1}{R_1} \quad \frac{1}{R_6} \quad G_1 \quad G_6$$

$$(G_1 + G_4 + G_6)u_{n1} \quad G_4 u_{n2} \quad G_6 u_{n3} = i_{s1} \quad i_{s6}$$

$$G_4 u_{n1} + (G_2 + G_4 + G_5)u_{n2} \quad G_5 u_{n3} = 0$$

$$G_6 u_{n1} \quad G_5 u_{n2} + (G_3 + G_5 + G_6)u_{n3} = i_{s6} + G_3 u_{s3}$$



$$\begin{aligned}(G_1+G_4+G_6)u_{n1} \quad G_4u_{n2} \quad G_6u_{n3} &= i_{s1} \quad i_{s6} \\ G_4u_{n1}+(G_2+G_4+G_5)u_{n2} \quad G_5u_{n3} &= 0 \\ G_6u_{n1} \quad G_5u_{n2}+(G_3+G_5+G_6)u_{n3} &= i_{s6}+G_3u_{s3}\end{aligned}$$

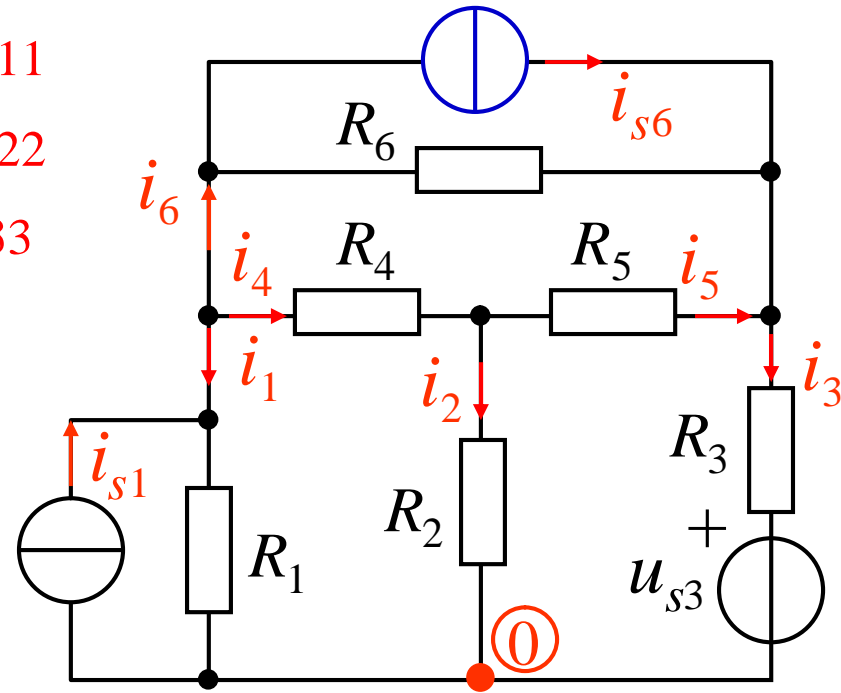
$$\begin{aligned}G_{11}u_{n1}+G_{12}u_{n2}+G_{13}u_{n3} &= i_{s11} \\ G_{21}u_{n1}+G_{22}u_{n2}+G_{23}u_{n3} &= i_{s22} \\ G_{31}u_{n1}+G_{32}u_{n2}+G_{33}u_{n3} &= i_{s33}\end{aligned}$$

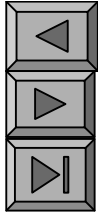
3.

- $G_{11} = (G_1+G_4+G_6)$

$$G_{22} = (G_2+G_4+G_5)$$

$$G_{33} = (G_3+G_5+G_6)$$

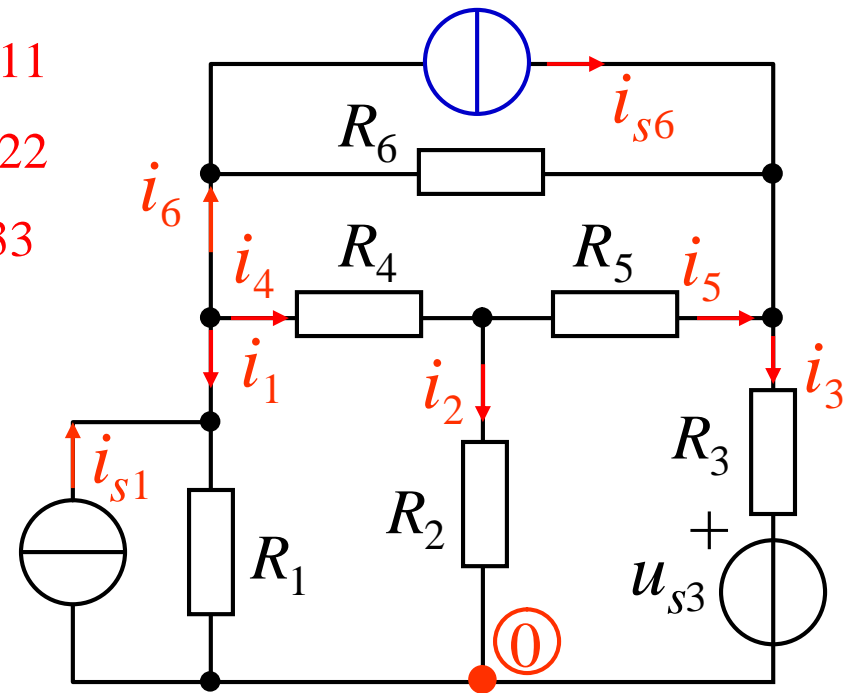


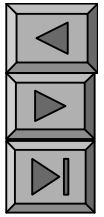


$$\begin{aligned}(G_1+G_4+G_6)u_{n1} \quad G_4u_{n2} \quad G_6u_{n3} &= i_{s1} \quad i_{s6} \\ G_4u_{n1}+(G_2+G_4+G_5)u_{n2} \quad G_5u_{n3} &= 0 \\ G_6u_{n1} \quad G_5u_{n2}+(G_3+G_5+G_6)u_{n3} &= i_{s6}+G_3u_{s3}\end{aligned}$$

$$\begin{aligned}G_{11}u_{n1}+G_{12}u_{n2}+G_{13}u_{n3} &= i_{s11} \\ G_{21}u_{n1}+G_{22}u_{n2}+G_{23}u_{n3} &= i_{s22} \\ G_{31}u_{n1}+G_{32}u_{n2}+G_{33}u_{n3} &= i_{s33}\end{aligned}$$

$$\begin{aligned}G_{12} &= G_{21} = -G_4 \\ G_{23} &= G_{32} = -G_5 \\ G_{13} &= G_{31} = -G_6\end{aligned}$$





$$(G_1 + G_4 + G_6)u_{n1} \quad G_4u_{n2} \quad G_6u_{n3} = i_{s1} \quad i_{s6}$$

$$G_4u_{n1} + (G_2 + G_4 + G_5)u_{n2} \quad G_5u_{n3} = 0$$

$$G_6u_{n1} \quad G_5u_{n2} + (G_3 + G_5 + G_6)u_{n3} = i_{s6} + G_3u_{s3}$$

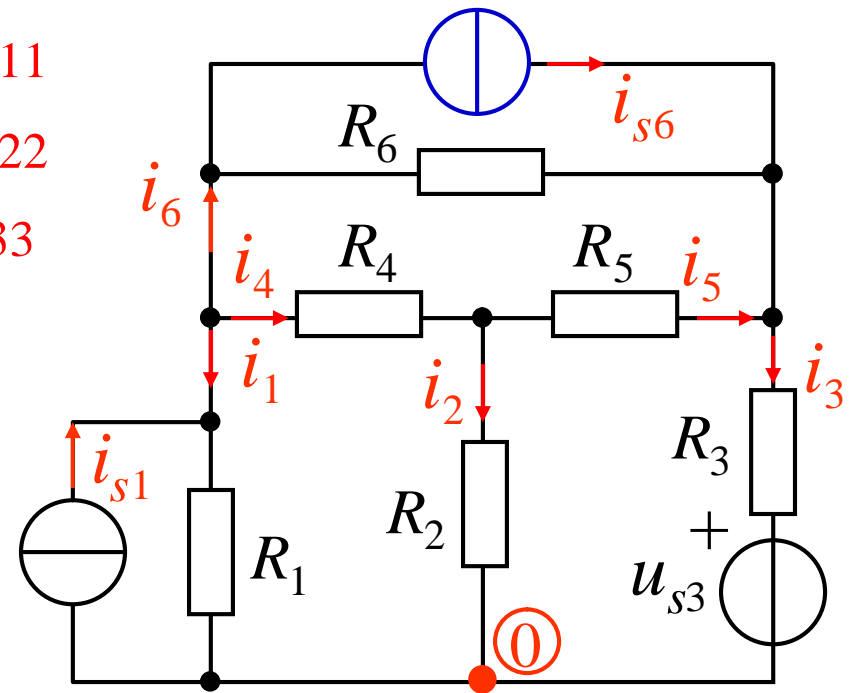
$$G_{11}u_{n1} + G_{12}u_{n2} + G_{13}u_{n3} = i_{s11}$$

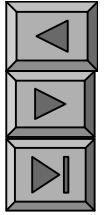
$$G_{21}u_{n1} + G_{22}u_{n2} + G_{23}u_{n3} = i_{s22}$$

$$G_{31}u_{n1} + G_{32}u_{n2} + G_{33}u_{n3} = i_{s33}$$

$$i_{s11} = i_{s1} - i_{s6} \quad i_{s22} = 0$$

$$i_{s33} = i_{s6} - G_3u_{s3}$$





4.

- $n - 1$

$$G_{11}u_{n1} + G_{12}u_{n2} + G_{13}u_{n3} + \dots + G_{1(n-1)}u_{n(n-1)} = i_{s11}$$

$$G_{21}u_{n1} + G_{22}u_{n2} + G_{23}u_{n3} + \dots + G_{2(n-1)}u_{n(n-1)} = i_{s22}$$

$$G_{31}u_{n1} + G_{32}u_{n2} + G_{33}u_{n3} + \dots + G_{3(n-1)}u_{n(n-1)} = i_{s33}$$

.....

$$G_{(n-1)1}u_{n1} + G_{(n-1)2}u_{n2} + G_{(n-1)3}u_{n3} + \dots + G_{(n-1)(n-1)}u_{n(n-1)} = i_{s(n-1)(n-1)}$$

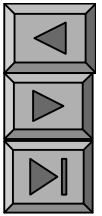
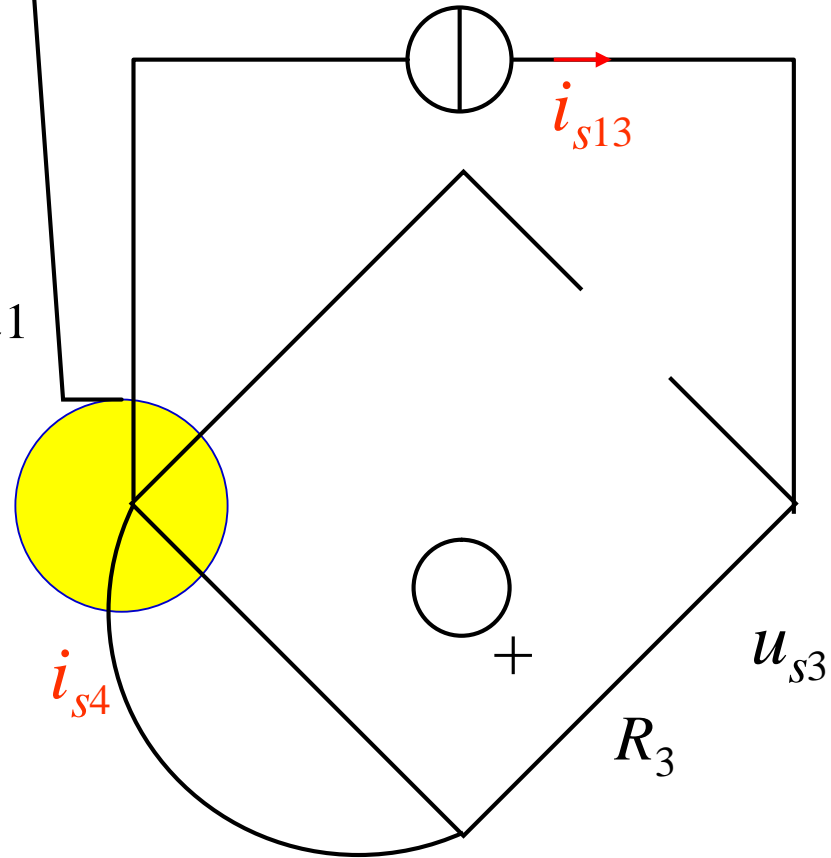
-

$$G_{ij} = G_{ji}$$

P71 3 5

①

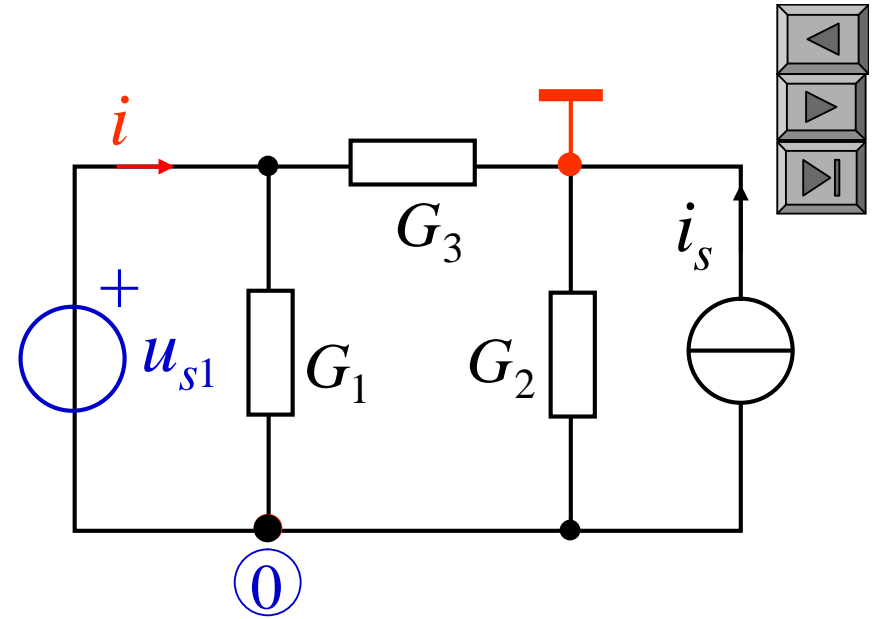
$$\begin{aligned}
 & : (G_1 + G_4 + G_8)u_{n1} \\
 -G_1 u_{n2} - G_4 u_{n4} & = i_{s4} - i_{s13} \\
 & : (G_1 + G_2 + G_5)u_{n2} \\
 -G_1 u_{n1} - G_2 u_{n3} & = 0 \\
 & : (G_2 + G_3 + G_6)u_{n3} \\
 -G_2 u_{n2} - G_3 u_{n4} & = i_{s13} - G_3 u_{s3} \\
 & : (G_3 + G_4 + G_7)u_{n4} - G_4 u_{n1} - G_3 u_{n3} \\
 & = G_3 u_{s3} + G_7 u_{s7} - i_{s4}
 \end{aligned}$$



3 6 ()

5.

P73 3 7



$$(G_1 + G_3)u_{n1} - G_3u_{n2} = i$$

$$-G_3u_{n1} + (G_2 + G_3)u_{n2} = i_{s2}$$

$$u_{n1} = u_{s1}$$

$$u_{s1}$$

$$u_{n1} = u_{s1}$$

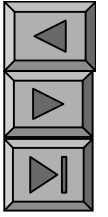
$$u_{n2}$$

$$(G_1 + G_3)u_{n1} - G_1u_{n0} = i$$

$$-G_1u_{n1} + (G_1 + G_2)u_{n0} = -i_{s2} - i$$

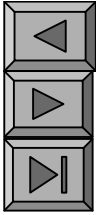
$$u_{n1} - u_{n0} = u_{s1}$$

3 7



6.

P74 3 8

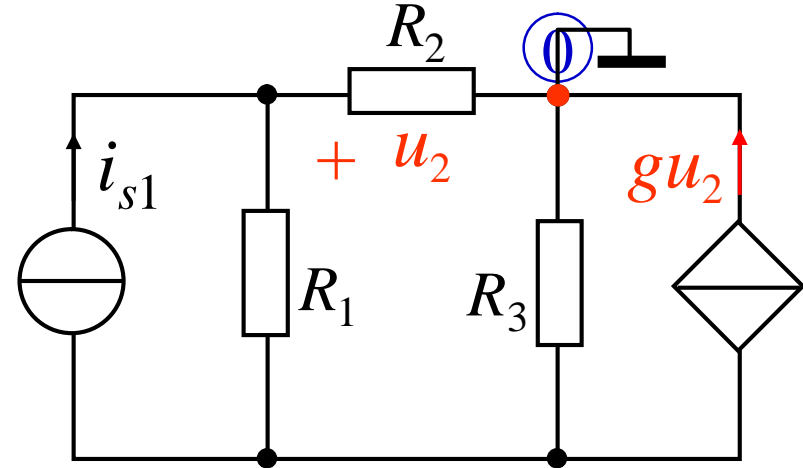


(1)

“0”

$$u_{n1} = u_2$$

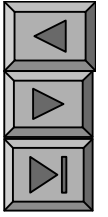
(2)



$$\therefore \left(\frac{1}{R_1} + \frac{1}{R_2} \right) u_{n1} - \frac{1}{R_1} u_{n2} = i_{s1} \quad (3)$$

$$\therefore \left(\frac{1}{R_2} + \frac{1}{R_3} \right) u_{n2} = -i_{s1} - g u_{n1}$$

$$\left(-\frac{1}{R_1} + g \right) u_{n1}$$



1. (“-”)

2. :

3.

4.

